Evaluation of Respirometric Data: Identification of Features That Preclude Data Fitting with Existing Kinetic Expressions

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Received July 24, 1995

biodegradation kinetic parameters for single organic compounds fication of these parameters, as well as the true growth yield, is discussed. Emphasis is placed on the preliminary assessment of y Several continuous and ba is discussed. Emphasis is placed on the preliminary assessment of
the data set to determine whether it is suitable for kinetic parame-
ter estimation (Grady, 1985). Since the introduc-
ter estimation. Careful preliminary e biodegradation of a single substrate by the culture tested. Both popularity. This can be attributed to the fact that these tech-
experimental and theoretical oxygen uptake curves are used to niques allow the collection of illustrate how various conditions can limit the utility of a given **data set. The effect of substrate inhibition, dual or multiple sub-** previous papers it has been demonstrated that respirometric **strate limited growth, inaccuracies in the initial conditions as-** data from batch growth experiments using acclimated bio-
sumed for curve fitting, and the use of poorly acclimated cultures mass may be used to estimate **sumed for curve fitting, and the use of poorly acclimated cultures** mass may be used to estimate the values of intrinsic kinetic are discussed. Techniques are presented which allow identification parameters characterizing are discussed. Techniques are presented which allow identification
of whether a data set is unsuitable and should not be used for
parameters characterizing the biodegradation of individual
parameter estimation. In additio

that maximal effluent concentrations be met for many syn- accomplished from a preliminary evaluation of the data. It thetic organic chemicals discharged from point-sources. To will also describe how initial estimates may be obtained for predict effluent concentrations from waste treatment unit op-
two of the parameters (Y and μ_{max} predict effluent concentrations from waste treatment unit op-
erations, adequate mass balances and rate terms for biotic also be applied to the evaluation of data on biomass growth and abiotic transformations must be developed and cali- or substrate depletion. brated. For biodegradable organic compounds, biotic transformation rates are often the most important and two pieces **MATHEMATICAL DEVELOPMENT** of information are necessary to calibrate them. First, an esti- *Respirometric Equations* mate of the fraction of biomass active in the degradation of tains two parameters (μ_{max} and K_s), whereas the Andrews equation for aerobic chemoheterotrophic microbial growth:

expression contains the same two, plus a third (K_i) . Thus, **The use of respirometric data for the evaluation of intrinsic** characterization of biodegradation kinetics involves quantinecessary to achieve the most exact parameter estimates (Dang *et al.,* 1989; Brown *et al.,* 1990). However, the data **INTRODUCTION** must be critically inspected before they are subjected to any curve fitting routine to ensure that they meet the criteria assumed in the Monod or Andrews equations. The purpose Increasingly stringent environmental regulations require of this paper is to illustrate how such an inspection can be also be applied to the evaluation of data on biomass growth

a given chemical is required. Second, estimates must be One of the key factors that allows the use of respirometric available for the specific parameters describing biotransfor- data for estimation of substrate biodegradation kinetics is mation of the chemical. The Monod (1949) and Andrews the fact that substrate consumption, biomass growth, and (1968) kinetic expressions are most commonly used to de- oxygen consumption are stoichiometrically linked according scribe biotransformation rates. The Monod expression con- to the following COD (chemical oxygen demand) balanced

$$
S - (1 - Y - Yp)O2 = YX + YpP
$$
 (1)

where S is the substrate concentration, X is the biomass concentration, P is the soluble microbial product concentration (all measured in COD units), *Y* is the biomass yield coefficient (mg biomass COD formed/mg substrate COD used), and *Yp* is the product yield coefficient (mg product COD formed/mg substrate COD used). Therefore, the rate of oxygen consumption, r_O , is linked to the rate of biomass growth, r_X , the rate of substrate consumption, r_S , and the rate of product formation, r_P , according to the following Parameter estimation is an iterative process. Using initial

$$
\frac{-r_{O_2}}{1 - Y - Y_p} = \frac{r_X}{Y} = \frac{r_p}{Y_p} = -r_S.
$$
 (2)

cumulative oxygen uptake at any time, O_{u_t} :

$$
O_{u_t} = S_o - S_t + X_o - X_t + P_o - P_t. \tag{3}
$$

tor all of the substrate COD removed is either converted parameter estimation algorithm is that the mathematical into biomass and microbial products or is oxidized to $CO₂$ model employed is an accurate description o into biomass and microbial products or is oxidized to $CO₂$. Use is made of this concept to allow computation of theoreti-
observations. Because the parameter estimation routine is cal oxygen consumption for the comparison with the actual unable to verify this assumption, it is the researcher's responmeasured oxygen consumption during nonlinear parameter sibility to evaluate the experimental data prior to parameter estimation. The estimation to determine whether they are adequately de-

data involves solution of the differential equations describing growth (Eq. (4)), substrate consumption (Eq. (5)), and prod- *Data Transformation to Facilitate Preliminary Evaluation* uct formation (Eq. (6)) (Dang *et al.,* 1989) thereby providing values of S_t , X_t , and P_t for substitution in Eq. (3). In these It is very difficult to examine an oxygen consumption equations, μ_t is the microbial specific growth rate (hr⁻¹) and b_t is the specific decay rate (hr⁻¹).

$$
\left(\frac{dX}{dt}\right)_t = \mu_t X_t - b_t X_t \tag{4}
$$

$$
\left(\frac{dS}{dt}\right)_t = -\frac{1}{Y} \mu_t X_t \tag{5}
$$

$$
\left(\frac{dP}{dt}\right)_t = -Y_p \left(\frac{dS}{dt}\right)_t.
$$
\n(6)

 $S - (1 - Y - Yp)O_2 = YX + YpP$ (1) expressed by either the Monod (Eq. (7)) or Andrews (Eq. (8)) expression.

$$
\text{Monod: } \mu_t = \mu_{\text{max}} \frac{S_t}{K_s + S_t} \tag{7}
$$

Andrews:
$$
\mu_{t} = \mu_{\max} \frac{S_{t}}{K_{s} + S_{t} + \frac{S_{t}^{2}}{K_{i}}}.
$$
 (8)

equation: estimates of the parameters *Y*, Y_p , μ_{max} , K_s , K_i , and *b* timedependent values for *S*, *X*, and *P* are obtained by solving Eqs. (4) – (6) simultaneously. These values are then substituted in Eq. (3) and the resulting predicted O_u profile is compared with the actual profile. Deviations between the actual and This means that oxygen consumption data provide exactly
the same information as biomass accumulation or substrate
consumption data. If growth occurs in a batch reactor with
a sealed aerobic environment, and all concentrat μ_{max} , K_s , and K_i . Parameter searching terminates when adequate agreement between the actual and predicted O_u profiles is obtained (i.e., when RSSE is sufficiently small). These parameters are called the best-fit parameters.

This states that in the sealed environment of a batch bioreac- It must be realized that the implicit assumption in any Typically, parameter estimation using batch respirometric scribed by the mathematical model employed. The following

curve by eye and ascertain whether the data are consistent with the assumptions implicit in the models depicted by Eqs. (4) through (8). One important assumption is that the bacteria are fully acclimated to the substrate of interest and able to consume it immediately. Therefore, any lag or acclimation period is minimal and all bacteria are assumed to be active. In addition, Monod or Andrews kinetics assume that there *is* only one factor limiting the growth rate, the substrate whose biodegradation kinetics are being evaluated. Luckily, these assumptions are much easier to evaluate if the oxygen consumption data are transformed in two alternative forms.

It is also difficult to ascertain whether the Monod (Eq. (7)) or Andrews (Eq. (8)) expression is the most accurate Before the equation can be solved, the dependency of the depiction of the effect of substrate concentration on μ . Theospecific growth rate on the substrate concentration must be retically, one should be able to employ only the Andrews equation during parameter estimation because it simplifies Thus, it can be seen that the rate of bacterial growth is if the Monod equation were more appropriate, then the curve absence of decay. fitting routine would simply return a large value for K_i . In Recognizing that: practice, however, a two-parameter fit (Monod) is much easier to accomplish than a three-parameter fit (Andrews). Con-
X sequently, it is beneficial to be able to choose the appropriate model prior to beginning the parameter estimation routine. This choice can be facilitated by the same type of data trans-
formation.

The rationale for the data transformation can be seen in the following. Taking the time derivative of all terms in Eq. (3) yields:

$$
\left(\frac{dO_u}{dt}\right)_t = -\left(\frac{dS}{dt}\right)_t - \left(\frac{dX}{dt}\right)_t - \left(\frac{dP}{dt}\right)_t.
$$
 (9)

Based on Eq. (2), the following substitution can be made:

$$
\left(\frac{dP}{dt}\right)_t = -Y_p \left(\frac{dS}{dt}\right)_t.
$$
\n(10)

growth phase and becomes significant only when substrate is almost completely removed. Therefore, decay has successfully been modeled with an inverse Monod function during parameter estimation (Dang *et al.,* 1989). However, when a batch growth experiment is terminated immediately after substrate respiration, changes in biomass concentration are The first comes from substitution of Eqs. (13) and (16) in predominantly determined by substrate consumption and cell Eq. (17): predominantly determined by substrate consumption and cell decay may be ignored. Thus, for purposes of data transformation, the following simplification may be made:

$$
\left(\frac{dS}{dt}\right)_t = -\frac{1}{Y}\left(\frac{dX}{dt}\right)_t.
$$
\n(11)

Equations (10) and (11) may be substituted in Eq. (9) to relate oxygen uptake rate to the rate of bacterial growth: Equation (18) reveals that μ may be determined solely from

$$
\left(\frac{dO_{u}}{dt}\right)_{t} = \frac{1 - Y_{p}}{Y} \left(\frac{dX}{dt}\right)_{t} - \left(\frac{dX}{dt}\right)_{t}
$$
\n
$$
= \frac{1 - Y_{p} - Y}{Y} \left(\frac{dX}{dt}\right)_{t}.
$$
\n(12)

Equation (12) can be solved for dX/dt to yield:

$$
\left(\frac{dX}{dt}\right)_t = \frac{Y\left(\frac{dO_u}{dt}\right)_t}{(1 - Y_p - Y)}.
$$
\n(13)

to the Monod equation when K_i is very large. In other words, directly related to the rate of oxygen consumption in the

$$
Y = \frac{X_t - X_o}{S_o - S_t} \text{ and } Y_p = \frac{P_t - P_o}{S_o - S_t},
$$
 (14)

$$
O_{u_t} = \frac{(1 - Y_p - Y)}{Y} (X_t - X_o), \tag{15}
$$

which can be solved for X_t :

$$
X_t = X_o + \frac{Y}{(1 - Y_p - Y)} O_{u_t}.
$$
 (16)

 $\left(\frac{dP}{dt}\right) = -Y_p\left(\frac{dS}{dt}\right)$. Equation (16) states that the amount of biomass grown is directly related to the amount of oxygen consumed. Two useful data transformations result directly form Eqs. (13) In batch growth experiments cell decay is minimal during the $\frac{1}{10}$ and the fact that the bacterial specific growth rate

$$
\mu_t = \frac{1}{X} \left(\frac{dX}{dt} \right)_t.
$$
 (17)

The sum of the following simplification may be made:\n
$$
\left(\frac{dS}{dt}\right)_t = -\frac{1}{Y} \left(\frac{dX}{dt}\right)_t
$$
\n
$$
\left(\frac{dS}{dt}\right)_t = -\frac{1}{Y} \left(\frac{dX}{dt}\right)_t
$$
\n<math display="block</p>

data on the rate of oxygen consumption and the total amount $\left(\frac{dO_u}{dt}\right)_i = \frac{1 - Y_p}{Y} \left(\frac{dX}{dt}\right)_i - \left(\frac{dX}{dt}\right)_i$ of oxygen consumed. Furthermore, since the residual substrate concentration is related to the amount of oxygen consumed (see Eq. (3)), Eq. (18) allows one to see how the substrate concentration affects the specific growth rate. The second useful transformation comes from rearranging Eq. (18) to yield:

$$
\left(\frac{dO_{u}}{dt}\right)_{t} = \frac{(1 - Y_{p} - Y)}{Y} \mu_{t}X_{0} + \mu_{t}O_{u_{t}}.
$$
 (19)

As will be demonstrated later the shape of the plot of $(dO_u/$ dt _t versus O_{u} is useful in identifying limitations during a batch growth experiment.

USE OF TRANSFORMED DATA PLOTS TO as time progresses. His expression is **EVALUATE ACCLIMATION AND IDENTIFY SUBSTRATE INHIBITION**

Impact of Acclimation

strate concentration, and cumulative oxygen consumption the rate of increase of growth activity of the cells over time that could be observed during the batch growth of a micro- (Kono, 1968). To simulate acclimation, Eq. (20) was used bial culture on a limiting carbon source. It is evident from in place of the Monod equation during acclimation, after Fig. 1 that growth may not commence immediately. Rather, which the Monod equation was applied until substrate was a lag phase may be observed wherein cells adjust to the new exhausted. Acclimation rate constants between 0.01 and 0.1 growth environment and growth is absent, followed by an hr^{-1} were used. In addition, a simulation was performed in acclimation phase during which an increasing number of the absence of acclimation, in which case exponential growth cells commence to grow and remove the substrate. Once all began immediately. cells are growing maximally, the exponential growth phase Figure 2A illustrates the respirometric response of a batch can be observed until the substrate becomes limiting and culture in the presence (solid curve) and absence (dashed declining growth ensues. Once all substrate is consumed, the curve) of acclimation. Examination of Fig. 2A indicates that cells enter the stationary phase. Recognition of the possible all of the curves are qualitatively similar. Consequently, it occurrence of the lag and acclimation phases is necessary would be almost impossible to tell from examination of the because neither the Monod nor Andrews equation is able to oxygen consumption curve whether acclimation had been model growth during those phases. If such phases are present occurring during a test. Transformation of the data set acin a data set, they must be eliminated before the remainder cording to Eq. (18) makes it immediately apparent that accliof the data set is used for parameter estimation. Because mation was occurring as presented in Fig. 2B. In the absence substrate utilization and biomass growth occur during the of acclimation, the specific growth rate starts immediately acclimation phase as illustrated in Fig. 1, elimination of that at a high value and declines as oxygen is consumed (i.e., as phase from the data set requires adjustment of the substrate substrate is consumed). However, in the presence of acclimaand biomass concentrations present at the start of the expo- tion, the specific growth rate rises initially, with the amount

In order to illustrate the use to which the transformed acclimation. plots can be put, a number of computer simulations were Ideally, researchers should avoid kinetic parameter estiperformed using the model depicted by Eqs. (3) through (8), mation with data from a growth experiment within which providing theoretical data of oxygen consumption versus significant acclimation had occurred. Thus, kinetic experitime. In all of those simulations, the following kinetic and ments should be commenced with a fully acclimated inocu-

stoichiometric parameters and initial conditions were used unless reported otherwise:

 $\mu_{\text{max}} = 0.1 \text{ hr}^{-1}$ $K_s = 1$ mg/liter as COD $K_i = 5, 10, 20, 50, 100, \infty$ mg/liter as COD $Y = 0.5$ mg biomass COD/mg substrate COD $Y_p = 0.05$ mg product COD/mg substrate COD $X_0 = 2.5$ mg/liter as COD $S_0 = 50$ mg/liter as COD.

In order to illustrate the impact of acclimation on the FIG. 1. Different phases that may be observed during microbial batch oxygen consumption curve for a batch bioreactor, use was growth on a single limiting nutrient. Biomass concentration, substrate concentration, and oxygen provides an empirical equation which mimics the effect of having more and more cells growing at their maximal rate

$$
\left(\frac{dX}{dt}\right)_t = \mu_{\text{max}}[X_t - (1 - \alpha t)X_0],\tag{20}
$$

Figure 1 illustrates profiles of biomass concentration, sub- where α is an acclimation rate constant which account for

nential phase. The method for doing so is discussed below. of oxygen and substrate consumed depending on the rate of

FIG. 2. The impact of an acclimation phase on oxygen consumption during batch growth and substrate mineralization. (A) Cumulative oxygen consumption profiles. (B) Specific growth rate profiles calculated with Eq. (18). The dashed lines represent the case without acclimation.

lum, which can easily be obtained by performing a prelimi- mation phase is not too long. With increasing acclimation nary respirometric test and harvesting the culture when it is phase lengths, more of the substrate consumption occurs in the exponential growth phase. during acclimation, providing only a very short period of

however, be used for kinetic parameter estimation provided tions, truncated data will not allow good estimation of μ_{max} . the data set is truncated to exclude the acclimation phase. *Identification of Substrate Inhibition* The end of the acclimation phase can be discerned most easily with the dO_u/dt vs O_u plot (Fig. 2B). When data are Another problem facing the experimenter during data Eq. (15). A similar equation can be derived that allows calcu-
lation of the substrate consumed:
 $\frac{1}{2}$
llustrates the

$$
O_{u_t} = \frac{(1 - Y_p - Y)}{Y} (X_t - X_o) = \frac{(1 - Y_p - Y)}{Y} \Delta X \quad (15'')
$$

$$
O_{u_t} = (1 - Y_p - Y)(S_t - S_o) = (1 - Y_p - Y)\Delta S.
$$
 (21)

Experiments with a significant acclimation phase can, subsequent exponential growth (Fig. 2B). Under such condi-

truncated in this way, the original conditions, S_0 and X_0 , analysis is the selection of the appropriate model for use in must be altered to reflect the conditions at the end of the parameter estimation. Figure 3A illustrates oxygen consumpacclimation phase because some substrate utilization and tion curves (in the absence of acclimation) associated with biomass growth occurs during the acclimation phase, as dis- Monod kinetics $(K_i = \infty)$ and with Andrews kinetics with cussed previously. The oxygen consumed during the accli- varying degrees of substrate inhibition (low *Ki* values repremation phase allows estimation of the substrate removed sent strong inhibition). As with Fig. 2A, it is evident from during this phase. Again, this value is derived most easily Fig. 3A that it would be very difficult to identify substrate from the dO_u/dt vs O_u plot (Fig. 2B). With knowledge of inhibition from examination of just an oxygen consumption the yield coefficients (see below), the biomass which was curve. Luckily, the type of transformation indicated by Eq. formed during the acclimation phase can be computed with (19), i.e., a plot of (dO_u/dt) _{*t*} vs O_u _{*n*} makes it much easier to

Figure 3B illustrates the dO_u/dt vs O_u profiles for the different degrees of inhibition kinetics depicted in Fig. 3A. All of the profiles are monotonically increasing functions of O_u until the substrate is nearly depleted. At that point the substrate concentration approaches K_s causing dO_v/dt to rapidly fall off and approach zero. In actual experiments, dO_v/dt *dt* will not decrease to zero. Rather, it will precipitously The values for biomass formed (ΔX) and substrate con- decrease to a fairly constant but very low dO_y/dt indicative sumed (ΔS) thus calculated must be added to and subtracted of endogenous oxygen consumption. The monotonic infrom the initial biomass and substrate concentrations, respec- crease in the profile is because during unrestricted growth tively, to obtain the X_0 and S_0 values at the onset of the (when $S > K_s$) the growth rate is a first order function of exponential growth. the biomass concentration. Because the oxygen consumption Truncation of the acclimation phase will provide sufficient rate is coupled to the growth rate (Eq. (2)) and the biomass data for kinetic parameter estimation provided that the accli- concentration is linked to the total oxygen consumed (Eq.

FIG. 3. The impact of the degree of substrate inhibition on the oxygen consumption rate during batch growth substrate mineralization. $K_i = 5$, 10, 20, 50, 100, or ∞ mg/liter. (A) Cumulative oxygen consumption profiles. (B) Oxygen consumption rate profiles.

(16)), the oxygen consumption rate is also an increasing only the carbon and energy source as the growth-limiting

downward. The presence of substrate inhibition is reflected kinetic parameter values. by upward concavity. This simple data transformation, there-
fore, makes clear the need to subject the data to a fitting *Oxygen Supply Limitation*

of data points collected during the experiment, with more rate and thus cannot be used for parameter estimation.
The impact of limiting oxygen delivery rates on oxygen

function of the cumulative oxygen consumption. With in-
substrate, a plot of dO_v/dt versus the cumulative oxygen creasing substrate inhibition (i.e., at decreasing values of K_i) consumption increases monotonically until the substrate be dO_u/dt is still an increasing function of O_u , although the comes limiting, at which time the plot drops precipitously. dependence is less than first order making the curve concave This is a very important characteristic of the plot and in this upward. section it will be demonstrated that deviations from that The *d*O_u/*dt* vs O_u curves, therefore, allow identification characteristic can be used to identify data sets which are not of the presence of substrate inhibition. In the absence of consistent with the assumptions inherent to the Monod and inhibition, the initial part of the plot will be linear or concave Andrews models. Such data sets cannot be used to obtain

routine that incorporates substrate inhibition kinetics. Figure 3B demonstrated that the rate of oxygen consump-
When experimental data are transformed, attention must
ion continually increases throughout a batch experimen When experimental data are transformed, attention must
be paid to the number of data points used to calculate each in the substrate becomes limiting at which time the rate be paid to the number of data points used to calculate each til the substrate becomes limiting, at which time the rate value of dO_y/dt . Because of the error associated with the drops rapidly However if the maximum rate a drops rapidly. However, if the maximum rate at which the experimental data, it is recommended that the oxygen con-
respirometer can deliver oxygen is less than the maximum sumption rate not be calculated using sequential data points. rate at which the bacteria need to use it, an artificial limit Rather, the use of three to five points is suggested. By shift-
is imposed upon the system which is imposed upon the system which results in a constant ing one point at a time, a smoothing of the slope can be growth phase rather than an exponentially increasing one. obtained that makes it much easier to identify the trends in Data collected under such a condition are not representative the data. The actual number used will depend on the quantity of the effect of substrate concentratio of the effect of substrate concentration on the specific growth

The impact of limiting oxygen delivery rates on oxygen consumption profiles is illustrated in Fig. 4 using experimen-**IDENTIFICATION OF FACTORS PRECLUDING** tal data from the batch mineralization of phenol. Figure 4A **PARAMETER ESTIMATION** illustrates the cumulative oxygen consumption data from two flasks with different maximal oxygen delivery rates. (Note In the preceding section it was illustrated how transformed that the initial substrate concentrations in the two flasks were data sets can be used to determine when acclimation has different, giving a different total oxygen consumption.) From been achieved and to identify the appropriate kinetic model Fig. 4A it is not immediately apparent that flask 1 had an describing the effect of substrate concentration on biodegra- oxygen transfer limitation, and in fact, both experimental dation. Figure 3B indicated that for a culture growing with curves could be fitted with a Monod equation describing

Α

0 10 15 20 25 30 50 0 5 Ó 100 150 Time (hrs) Cumulative Oxygen Consumption (mg/L) **FIG. 4.** The impact of an oxygen delivery limitation on oxygen consumption rate during batch growth substrate mineralization experiments. Flask

1, solid line; flask 2, dashed line. (A) Cumulative oxygen consumption profiles. (B) Oxygen consumption rate profiles. Note that the two flasks received different initial substrate concentrations.

transfer limited the growth rate in flask 1. This can clearly sumption rates, are maximal. The following expressions for be seen much more easily in Fig. 4B which illustrates the *S** were derived for Monod and Andrews kinetics, respecchange in oxygen consumption rate as a function of the tively: cumulative oxygen consumption for both flasks. Flask 2 followed the expected profile illustrated in Fig. 3B. Flask 1, however, had a period of constant oxygen consumption rate indicative of an oxygen transfer limitation. Parameters obtained by fitting curve 1 to the Monod equation are not valid and should be discarded because the assumption of a single $S_{\text{Andrews}}^* =$ substrate limitation inherent to the Monod equation was violated.

In order to ensure that all experimental data are valid and can be used for parameter estimation, the oxygen delivery system in the respirometer should be adjusted so that it is capable of delivering oxygen at a rate in excess of the maximum rate that the culture will experience. An estimate of that maximum rate can be made using likely values for the kinetic parameters. Recognizing that at any time the biomass Using preliminary estimates of K_s , K_i , and Y , values for S^* concentration $X = X + Y(S - S)$ For (11) and (17) can be calculated and used to find the maximum concentration $X_t = X_0 + Y(S_0 - S_t)$, Eqs. (11) and (17) can

$$
\left(\frac{dS}{dt}\right)_t = -\frac{1}{Y}\mu_t(X_0 + Y(S_0 - S_t)).
$$
 (22)

nod or Andrews rate term (Eqs. (7) and (8)) to yield an because this will result in a respirogram with less resolution. expression for dS/dt with *S* as the sole dependent variable. The researcher can also easily evaluate the maximum O_2 By taking the second derivative of *S* with respect to time, transfer rate achievable by a given experimental system, by for S^* can be obtained. These values represent the substrate biological activity ensures that O_2 transfer will be limiting, concentrations during the growth experiment at which the and its value can be observed from the dO_u/dt vs O_u plot.

growth. Detailed inspection, however, revealed that oxygen substrate transformation rates, and hence the oxygen con-

$$
S_{\text{Monod}}^{*} = -K_{s} + \sqrt{K_{s}^{2} + K_{s}\left(S_{o} + \frac{X_{o}}{Y}\right)}
$$
(23)

B

$$
\frac{-K_s + \sqrt{K_s^2 + K_s\left(S_o + \frac{X_o}{Y}\right)\left[\left(S_o + \frac{X_o}{Y}\right)\frac{1}{K_i} + 1\right]}}{\left[\left(S_o + \frac{X_o}{Y}\right)\frac{1}{K_i} + 1\right]} \tag{24}
$$

be combined to yield: u is the corre-
uptake rate, using Eqs. (22) and (7) or (8). The corresponding oxygen consumption rate can then be calculated with Eq. (2).

The oxygen delivery rate of the apparatus should be set at a safe multiple of the calculated maximum oxygen consumption rate to avoid oxygen limitations. Care should be The μ_t term is subsequently replaced by the appropriate Mo- taken, however, to not set the oxygen delivery rate too high and solving the equation for the condition $d^2S/dt^2 = 0$, values performing a test with excess biological activity. The excess

FIG. 5. The impact of $NH_4^+ - N$ limitation on the oxygen consumption FIG. 5. The impact of NH₄ – N limitation on the oxygen consumption
rate during batch growth on a single substrate as calculated by modeling.
NH₄ – N was assumed to be present in excess, or at 4, 2, 1 (dashed line), $\frac{1}{2}$, $\frac{1}{2}$,

organic substrate and the nitrogen source $(NH_4^+ - N)$ were

$$
\mu_t = \mu_{\max} \frac{S_{1t}}{K_{s_1} + S_{1t}} \frac{S_{2t}}{K_{s_2} + S_{2t}} \tag{25}
$$

the N dose exceeds the stoichiometrically required amount by as much as fourfold, oxygen consumption rates are impacted. This means that any kinetic parameters obtained by fitting with a single substrate model would be incorrect. Second, when the N dose is less than the nonlimiting amount, the dO_u/dt profiles qualitatively change. Oxygen consumption rates level off too soon and gradually decrease to zero. This means that any kinetic parameters obtained by fitting with a single substrate model would be incorrect. Third, when the N dose is less than the stoichiometrically required amount, the total oxygen consumed is less than expected. Consequently, atypically high yield values are calculated (see Eq. (25) below). Such high yields provide an easy means for identifying severe nutrient limitation. The degree of impact of a second nutrient limitation on the substrate and However, to be conservative, it is recommended that all nutrients be provided in at least a 10-fold stoichiometric excess to avoid the impact of a second limitation on the *Nutrient Limitation* biodegradation and resulting oxygen consumption profiles.

A second common growth limitation that can occur during The impact of a nutrient limitation on experimental oxyrespirometric experiments is due to deficiencies in the min- gen consumption profiles is illustrated in Fig. 6. The data eral composition of the medium used. The ability of the were collected from the batch growth mineralization of tolumedium to allow unrestricted growth should be verified by ene (initial concentration of 100 mg/liter as COD) by an the researcher based on preliminary knowledge of the yield enrichment culture. The inoculum size to all flasks was idenand stoichiometry of the bacterial cell. In order to illustrate tical, while different amounts of a mineral salts solution the impact of an inorganic nutrient limitation, simulations were added to each flask. The full-strength mineral salts were performed using a kinetic model in which both the solution provides stoichiometrically sufficient micro- and organic substrate and the nitrogen source $(NH_4^T - N)$ were macronutrients to allow mineralization of 5000 mg/liter as growth limiting. Instead of the single substrate limitation COD of an organic substrate (Daigger, 1979) COD of an organic substrate (Daigger, 1979). The mineral (Eq. (7)), a dual substrate limitation model was used to com-
pute the specific growth rate (Droop, 1973):
 $50-5-$ or 0.5-fold the stoichiometrically required dose for 50-, 5-, or 0.5-fold the stoichiometrically required dose for mineralization of 100 mg/liter as COD of toluene. Figure 6A clearly indicates the nutrient limiting effect when only 0.5-fold the stoichiometrically required dose was added. The observed oxygen consumption rates during mineralization wherein S_1 and K_{s_1} refer to the concentration of and the were significantly lowered, as was the total cumulative oxy-
affinity for the organic substrate and S_2 and K_{s_2} refer to the gen consumption. This ve affinity for the organic substrate and S_2 and K_{s_2} refer to the gen consumption. This very low oxygen consumption, or concentration of and affinity for NH₄⁺ – N, respectively, A conversely very high apparent yi concentration of and affinity for $NH_4^+ - N$, respectively. A conversely very high apparent yield (see Eq. (25) below), is typical K_{s_2} values of 0.5 mg/liter as NH₄⁺ – N was assumed. indicative of incomplete substrate respiration. The difference Based on the empirical formula $C_5H_7O_2N$ for bacterial mass in the oxygen consumption profiles for the cases in which (Hoover and Porges, 1952), a constant ratio of 0.15 g N the nutrient excess was 50- or 5-fold is less apparent. Both consumed per gram of substrate COD consumed was calcu- curves plateaued at approximately the same total cumulative lated for balanced microbial growth and no substrate storage oxygen uptake indicating complete substrate respiration. was assumed to occur during N limitation. Some indication of lower growth rates, however, was appar-The impact of an increasing $NH_4^+ - N$ limitation resulting ent in the 5X curve. This is more evident in Fig. 6B illustratfrom these simulations is illustrated in Fig. 5. At the onset ing again the utility of the transformed data plot. Thus, even of growth, $NH_4^+ - N$ was either provided in great excess when nutrients were provided in 5-fold excess, growth rates (using the single substrate limitation model) or was provided were reduced, with the result that Monod kinetic parameters at 4, 2, 1, 0.5, or 0.25 times the stoichiometrically required obtained under these experimental conditions would not dose. Figure 5 illustrates three key points. First, even when truly reflect the kinetics of biodegradation under a single

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16 14

Cumulative Oxygen Uptake (mg/L) 50X 12 50 dOu/dt (mg/L.hr) 10 40 8 30 6 $0.5X$ 20 10 $0.5X$ $\overline{\mathbf{c}}$ 0 $\mathbf 0$ \overline{a} $\bf 6$ 8 40 $\mathbf 0$ 10 12 $\mathbf 0$ 20 60 80 14 Time (hrs) Cumulative Oxygen Uptake (mg/L)

FIG. 6. The impact of a nutrient limitation on the oxygen consumption rate as observed during batch growth experiments on a single substrate. Nutrients were provided at 0.5, 5, or 50 times the stoichiometric amount. (A) Cumulative oxygen consumption profiles. (B) Oxygen consumption rate profiles.

substrate limitation. Better estimates for the single substrate more difficult to properly quantify the individual Monod pa-

embodied in the Monod or Andrews equations are no longer 1988). valid. Further data fitting should be abandoned because neither the Monod or Andrews equation are adequate models **OTHER USES OF TRANSFORMED DATA PLOTS** to describe these dual or multiple limitation phases. Rather,
after identification of the cause of the limitation, the experi-
ment should be revised to remove the additional limitation
limitation and repeated.

Inappropriate S_o Value

How an oxygen transfer limitation can be identified from a region of constant oxygen uptake rate in a plot of dO_u/dt was illustrated earlier. Other factors, however, can also affect the shape of the dO_u/dt curve and thus care must be exercised while interpreting such plots. One of those factors is the affinity of the microorganisms for the substrate as reflected in the value of the half-saturation coefficient, *Ks*, and more particularly the initial substrate concentration used in an experiment relative to that half-saturation coefficient. To illustrate this point, simulations were performed using a model incorporating Monod kinetics and Fig. 7 illustrates the different oxygen consumption rate profiles obtained when K_s was varied while holding S_0 constant. From this figure it can be seen that as K_s becomes the fact that as the ratio of S_0 to K_s becomes smaller, it becomes cod.

growth parameters on toluene were derived from the experi- rameters by nonlinear curve fitting to experimental data ment wherein nutrients were at 50-fold excess. This experi- (Wang, 1988). Therefore, the presence of a constant or quasimental curve allowed fitting with the Monod equation in a constant phase in the dO_u/dt vs O_u curve is undesirable and model which accounts for the partitioning of toluene between should be avoided. In such cases, the experimental design need the gaseous and the aqueous phase (Naziruddin *et al.,* 1995). to be redone so that a growth experiment with a higher initial Whenever a second limitation is observed due to oxygen substrate concentration is performed. For optimum parameter transfer or nutrient limitation, the proposed μ/S relationships identifiability, the S_0/K_s value should be at least 1.0 (Wang,

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FIG. 8. The impact of the degree of substrate inhibition and the estimate of the initial biomass concentration on the calculated specific growth rate profiles. (A) $K_i = \infty$, (B) $K_i = 100$, (C) $K_i = 20$, (D) $K_i = 5$. In all panels, profiles from bottom to top were calculated with X_0 estimates of 10, 5, 2.5 (dashed line), 1, 0.5, and 0.1 mg/liter as COD. The exact initial biomass concentration was 2.5 mg/liter.

that preclude use of a data set for parameter estimation, there as 50% (Fig. 3B) at increasing levels of inhibition. Nevertheare obtaining initial estimates for μ_{max} and *Y*, and verification for subsequent curve fitting. that the initial biomass concentration, X_0 , used during curve Y can be estimated from the total oxygen consumption at

dt vs O_u curve is μ_t . For Monod kinetics, $\mu_t = \mu_{\text{max}}$ when *S* or soluble microbial products. Therefore, μ_p is calculated as $\gg K$. Therefore, the initial slope of the *dO* /*dt* vs O, profile the ratio of the $\geq K_s$. Therefore, the initial slope of the dO_v/dt vs O_u profile
provides a good estimate of μ_{max} for Monod kinetics. How-
ever when significant substrate inhibition occurs (i.e., when
 $\frac{O_{u_p}}{Q_{u_p}}$ and Y_p , ever, when significant substrate inhibition occurs (i.e., when Andrews kinetics apply), accurate estimates of μ_{max} cannot be readily obtained because the specific growth rate is depressed at higher substrate concentrations. As a rough approximation, the construction of a line that goes through the origin and is tangential to the dO_u/dt vs O_u curve near its highest value is suggested. Its slope can be used as a first O_{u_p} can be obtained from the O_u vs *t* curve as the oxygen estimate of μ_{max} . This estimate is fair at low substrate inhibi-
tion, but may underestimate the true μ_{max} value by as much cern. It is easier to estimate O_u, from the dO_u/dt vs O_u curve, tion, but may underestimate the true μ_{max} value by as much

are other more positive uses of them as well. Among them less, it should still provide an adequate initial $\mu_{\rm max}$ estimate

fitting is indeed correct. the onset of the plateau in oxygen consumption O_{u_p} , after which the endogenous phase occurs. First, however, Y_p *Initial Estimation of* μ_{max} *and Y* must be estimated from the soluble COD fraction remaining Examination of Eq. (19) reveals that the slope of the *d*O_u/ in the respirometric at the plateau. That COD is comprised vs O curve is u. For Monod kinetics $\mu = \mu$ when S of soluble microbial products. Therefore, Y_p i

$$
Y = 1 - \frac{\mathcal{O}_{\mathbf{u}_{\mathrm{p}}}}{S_{\mathrm{o}}} - Y_{\mathrm{p}}.
$$
 (26)

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FIG. 9. The identification of a wrong *X*^o estimate and its impact on the best fit parameters estimates for a batch growth substrate mineralization experiment. (A) Cumulative oxygen consumption profiles and best fit curves. (B) Calculated specific growth rate profiles. The smooth continuous lines are the predicted curves from the model fits.

as the O_{u_p} value obtained by extending the rapidly falling estimation of the best fit kinetic parameters is illustrated in region of the curve to the abscissa as presented in Fig. 3B. Fig. 9. The oxygen consumption da

during parameter estimation. To calculate μ according to
Eq. (18), values for Y, Y_p, and X_o must be known. Y and Y_p (Brown *et al.*, 1990) were applied with those values to esti-
are estimated independently as de theoretical oxygen consumption plot corresponding to those upon μ_{max} , K_s , and K_i , it may be used to check the accuracy depend theoretical oxygen consumption plot corresponding to those of the estimate of *X* by of the estimate of X_0 by examining the shape of the resulting μ vs O_u curve.

The impact of an incorrect X_0 estimate is the most apparent creasing oxygen consumption. If the value of X_0 is larger will lie above the correct profile and fall toward it. The

The impact of an incorrect X_0 value on the subsequent goodness of fit associated with a given set of parameter

Fig. 9. The oxygen consumption data in Fig. 9A were obtained from the mineralization of 100 mg/liter as COD of *Verification of the Initial Biomass Concentration, X_o* phenol by an enrichment culture. The initial inoculum con-The other useful transformation of the experimental data centration was measured experimentally as 4.8 mg/liter and
allows evaluation of the accuracy of the X_0 value to be used Y and Y_p were measured at the end of are estimated independently as described above, while X_0 , mate μ_{max} and K_s for the Monod equation. The resulting or a best estimate thereof, is typically measured at the begin-
parameter values were $\mu_{\text{max}} =$ or a best estimate thereof, is typically measured at the begin-
ning of the experiment. Because Eq. (18) does not depend COD/liter which resulted in a RSSE value of 35.36. The The dashed curve in Fig. 8 illustrate the shape of the μ mation of Eq. (18) is made for both the experimental data of the sysociated with different degrees of substrate inhibi-
of the fitted curve, it becomes apparent profiles associated with different degrees of substrate inhibi- and the fitted curve, it becomes apparent that the X_0 value tion when the value of X_0 is exact. The solid curves illustrate was in error. This can be s tion when the value of X_0 is exact. The solid curves illustrate was in error. This can be seen in Fig. 9B in which the smooth how the calculated μ profiles behave for incorrect X, values curve corresponds to the fit how the calculated μ profiles behave for incorrect X_0 values. Curve corresponds to the fitted curve and the jagged curve The impact of an incorrect X_0 estimate is the most apparent corresponds to the data. The fa early in the profile because the term containing X_0 in the initially indicates that X_0 was too small. Adjustments were denominator of Eq. (18) becomes less significant with in-
creasing oxygen consumption. If the value of X_0 is larger tively flat, yielding and X_0 value of 8.0. The nonlinear curve than the true value, the curves of μ vs O_u will lie below the fit was then repeated giving a μ_{max} value of 0.571 hr⁻¹ and correct μ profile and rise toward it. Conversely, if the as- a K_s value of 4.08 mg COD/liter, which resulted in a much sumed X_0 value is smaller than the true value, then the curves lower RSSE value of 6.48. Examination of Fig. 9A reveals will lie above the correct profile and fall toward it. The that it is very difficult to discern a impact of incorrect X_0 values is easily discernible when sub- fit 1 and best fit 2 when plots of O_u versus time are examined strate mineralization obeys Monod kinetics (Fig. 8A), or by eye. However, examination of Fig. 9B illustrates that when substrate inhibition is small (Fig. 8B). When substrate after the transformation of Eq. (18) is applied, the superiority inhibition is large, however, incorrect X_0 values are harder of best fit 2 is clearly evident. This illustrates two important to discern, especially if they are larger than the true value points. First, use of an incorrect X_0 value during curve fitting (Fig. 8D). The sult in incorrect estimates of μ_{max} and K_s . Second, the

plots than in plots of oxygen consumption versus time, even
the Technical University of Budapest and Clemson University.
though parameter estimates were obtained by fitting the
latter.

This paper addressed the preliminary evaluation of respi- compounds. *Water Environ. Res.* **64,** 890–900. rometric data obtained during biodegradation of organic Andrews, J. F. (1968). A mathematical model for the continuous culture compounds in batch reactors. Based on theoretically exact of microorganisms utilizing inhibitory substrates. *Biotechnol. Bioeng.* **10,** respirometric profiles, how those profiles are impacted by $707-723$.
substrate inhibition puttiont limitation oxygen delivery lim Brown, S. C., Grady, C. P. L., Jr., and Tabak, H. H. (1990). Biodegradation substrate inhibition, nutrient limitation, oxygen delivery lim-
itation, the presence of an acclimation phase, and incorrect
estimates of the active inoculum size was examined. The
examined. The
principal Γ Γ (1070) esumates of the active moculum size was examined. The Daigger, G. T. (1979). The Interaction between Physiological Adaptation impact of these complicating factors is frequently difficult and Transport Response for Pseudomo to discern in the untransformed data set, but can be detected *Dynamic Modeling of Microbial Growth.* Ph.D. thesis. Purdue University, with greater ease when the data are transformed and the Lafayette, IN.
oxygen consumption rate profile or the specific growth rate Dang, J. S., Harvey, D. M., Jobbágy, A., and Grady, C. P. L., Jr. (1989). oxygen consumption rate profile or the specific growth rate Dang, J. S., Harvey, D. M., Jobbágy, A., and Grady, C. P. L., Jr. (1989).

Evaluation of biodegradation kinetics with respirementic data. Res. J. profile is inspected. Such evaluation can be carried out fairly
simply using a spreadsheet program and should be executed
prior to subjecting the data set to nonlinear curve fitting. This
 $\frac{1}{3}$, 209–214. preliminary evaluation allows the investigator to examine Grady, C. P. L., Jr. (1985). Biodegradation: Its measurement and microbiowhether the conditions implicit to the two commonly used logical basis. *Biotechnol. Bioeng.* **27**, 660–674. expressions to describe substrate limited microbial growth, Hoover, S. R., and Porges, N. (1952). Assimilation of dairy wastes by the Monod and Andrews equation, are met. Such examina-

tion ensures that the reported kinetic parameters truly reflect

tion. Sewage Ind. Wastes 24, 306–312. tion. *Sewage Ind. Wastes* 24, 306–312.
the kinetics of degradation under single substrate limited Kono, T. (1968). Kinetics of microbial cell growth. *Biotechnol. Bioeng*. 10, the kinetics of degradation under single substrate limited
conditions by an acclimated culture.
Monod, J. (1949). The growth of bacterial cultures. Ann. Rev. Microbiol.

At the time of this work, B.F.S. and R.M.C. were research associates/ of respirometry. *Water Environ. Res.* **67,** 151–158. assistant professors, and A.J. was a postdoctoral research associate in the Wang, X. (1988). *The Development of a Nonlinear Parameter Estimation* Funding for this research was in part by the United States–Hungarian SC.

estimates is often more easily discerned in transformed Science and Technology Joint Fund through Grant 91b-192 for cooperation

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REFERENCES

- **CONCLUSION** Aichinger, G., Grady, C. P. L., Jr., and Tabak, H. H. (1992). Application of respirometric biodegradability testing protocol to slightly soluble organic
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	-
	- **3,** 371–394.
- **ACKNOWLEDGMENTS** Naziruddin, M., Grady, C. P. L., Jr., and Tabak, H. H. (1995). Determination of biodegradation kinetics of volatile organic compounds through the use
- Department of Environmental Systems Engineering at Clemson University, *Technique for Use with Biodegradation Data.* M.S. thesis, Department where C.P.L.G. is the R. A. Bowen professor of environmental engineering. of Environmental Systems Engineering, Clemson University, Clemson,